

Since for $|x| < 1$ we have

$$\log(1+x) = x - \frac{x^2}{2} + \frac{x^3}{3} + \dots$$

we may write $\log(1+x) = x + O(x^2)$.